

$01^p 001^p 0$

$uvxyz$

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$0^p 1^p 0^p 0^p 1^p 0^p$

$ww^R$ :  
 $w$  is a  
Palindrome

Show  $L$  is not CFL.

know  $J$  is a CFL  
"  $M$  is not

$$L \cup J = M$$

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Show  $L$  is a CFL.

$$A \cup B = L$$

$A, B$  are CFL's

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$A, B$  are CFL's.

$A \cap B?$

$$A_{TM} = \{ \langle M, w \rangle \mid$$

$M$  is a TM that accepts  
 $w$

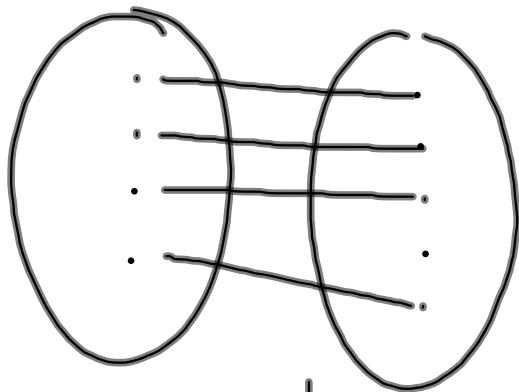
$A_{TM}$  is recognizable  
construct TM  $U$ .

$U =$  on input  $\langle M, w \rangle$  where  
 $M$  is a TM and  $w$  is a string.

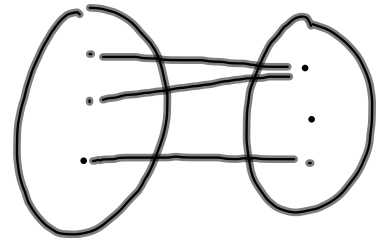
1. simulate  $M$  on  $w$
2. if  $M$  enters an accept state, accept  
if  $M$  enters a reject state, reject.

# Infinite Sets countable/uncountable

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one-to-one  
! onto



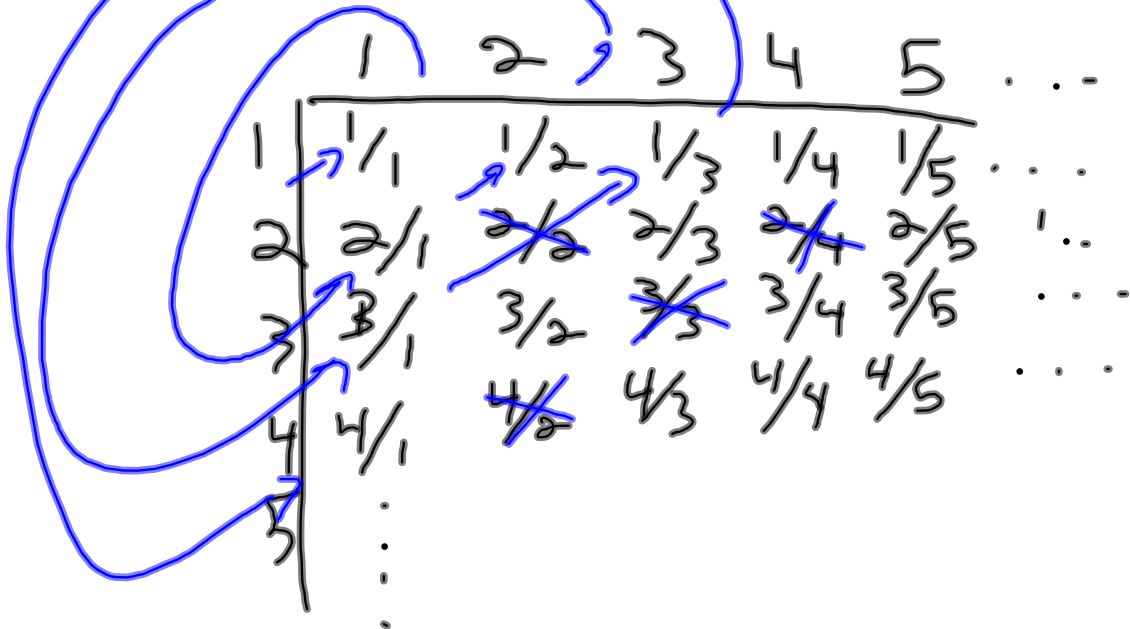
! one-to-one

$$E = \{2, 4, 6, \dots\}$$

$$f: \mathbb{N} \rightarrow E$$

$$f(n) = 2 \cdot n$$

$$\mathbb{Q} = \left\{ \frac{m}{n} \mid m, n \in \mathbb{N} \right\}$$



Uncountable

$\mathbb{R}$

Suppose  $\mathbb{R}$  is countable

| $n$ | $f(n)$                |
|-----|-----------------------|
| 1   | 0. <u>0</u> 1011...   |
| 2   | 3.14 <u>1</u> 59...   |
| 3   | 0.999 <u>9</u> 999... |
| 4   | 35.362 <u>1</u> 7806. |

$$x = 0.1232\dot{\phantom{2}}$$