

$$L = \{ w \mid w \in \{a, b, c\}^* \\ \text{number of a's} < \# \text{ b's} \\ \text{and } \# \text{ of a's} < \# \text{ c's} \}$$

L is not Context free.

Suppose L is context free, w/ pumping length p.

Choose $s = a^p b^{p+1} c^{p+1}$

By the P.L. we can split s into 5 parts, uvxyz

vxy can contain at most 2 ^{distinct types} symbols.

$$|vxy| \leq p$$

Case 1: v and y ~~are all~~ ^{contain} a's
 so v and y contain no c's
 so uv^2xy^2z has at least as many a's as c's
 so $uv^2xy^2z \notin L$

Case 2: v and y contain no a's
 so uv^0xy^0z contains fewer of b's or c's (or both) than a's and so is not in L

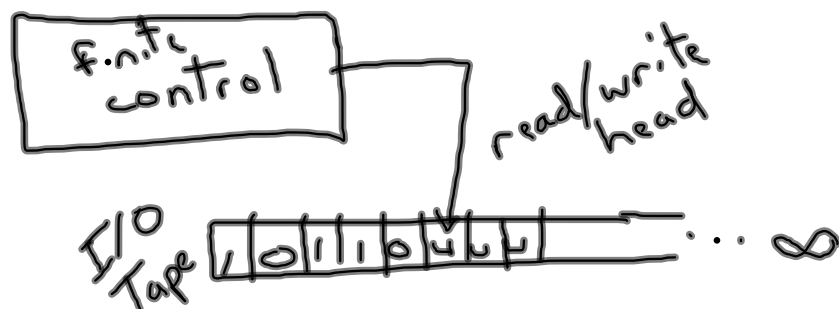
So L is not a CFL.

$$\begin{array}{l} A \rightarrow B \\ \neg B \rightarrow \neg A \end{array} \quad \begin{array}{l} \cancel{B \rightarrow A} \\ \neg A \rightarrow \neg B \end{array}$$

Turing Machines

Church - Turing Thesis

Turing Machines can compute any computable function.



- read/write from tape
- move r/w head left/right
- accept/reject states (immediate)
- start the r/w head on the left end
- special "blank" symbol \sqcup , \perp
- input str starts on left end of the tape

$$L = \{ w \# w \mid w \in \{0,1\}^* \}$$

