

Cook and Levin

boolean formula

- variables: x, y, z

- operations: \wedge, \vee, \neg

$\rightarrow x$ \bar{x}
 $!x$ $\sim x$

Is there an assignment of t or f values to the variables that makes the formula true? (satisfying assignment)

If so, the formula is satisfiable.

$x \wedge y$ yes $x=t, y=t$
 $x \wedge \bar{x}$ no

$SAT = \{ \langle \phi \rangle \mid \phi \text{ is a satisfiable boolean formula} \}$

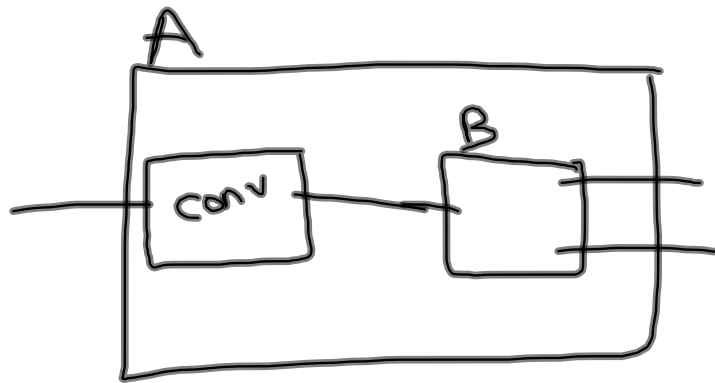
Cook-Levin Thm:

$SAT \in P \iff P=NP$

NP-complete (NPC)

if an NPC problem is solvable
in polynomial time, then all
NP problems are solvable in polynomial
time.

A reduces to B



A function $f: \Sigma^* \rightarrow \Sigma^*$
is a polynomial time computable
function if some polynomial time
TM exists that halts w/
just $f(w)$ on its tape, when started
on any input w .

Language A is poly-time reducible
to language, $A \leq_p B$ if

a poly-time function f exists

where for every w

$$w \in A \text{ iff } f(w) \in B$$

if $A \leq_p B$ and $B \in P$ then $A \in P$

3-SAT

- ① formulas are in conjunctive normal form
 - literals: x, \bar{x}
 - terms: literals or'd together
 $(x \vee \bar{y}) \quad (x \vee y \vee z)$
 - formulas: terms and'd together
 $(x \vee y) \wedge (\bar{x} \vee \bar{y})$

AND

- ② each term contains exactly 3 literals.
- \nwarrow
 \nearrow
 3CNF

$$3SAT = \{ \langle \phi \rangle \mid \phi \text{ is a satisfiable } 3\text{cnf formula} \}$$

$$3SAT \leq_p \text{ CLIQUE}$$

$\{ \langle G, k \rangle \mid G \text{ is an undir. graph that contains a } k\text{-clique} \}$

