

$$m, n \in \mathbb{Z} \quad m \leq n$$

$n - m + 1$ integers in the
list from m to n

$$3, 4, 5, 6, 7, 8, 9, 10$$

$$10 - 3 + 1 = 8$$

How many 3 digit #'s are divisible by 3?

100, 101, 102, 103, 104, 105, 106, ..., 999
 ↑ ↑ ↑
 3·34 3·35 3·333

34, 35, 36, ..., 333

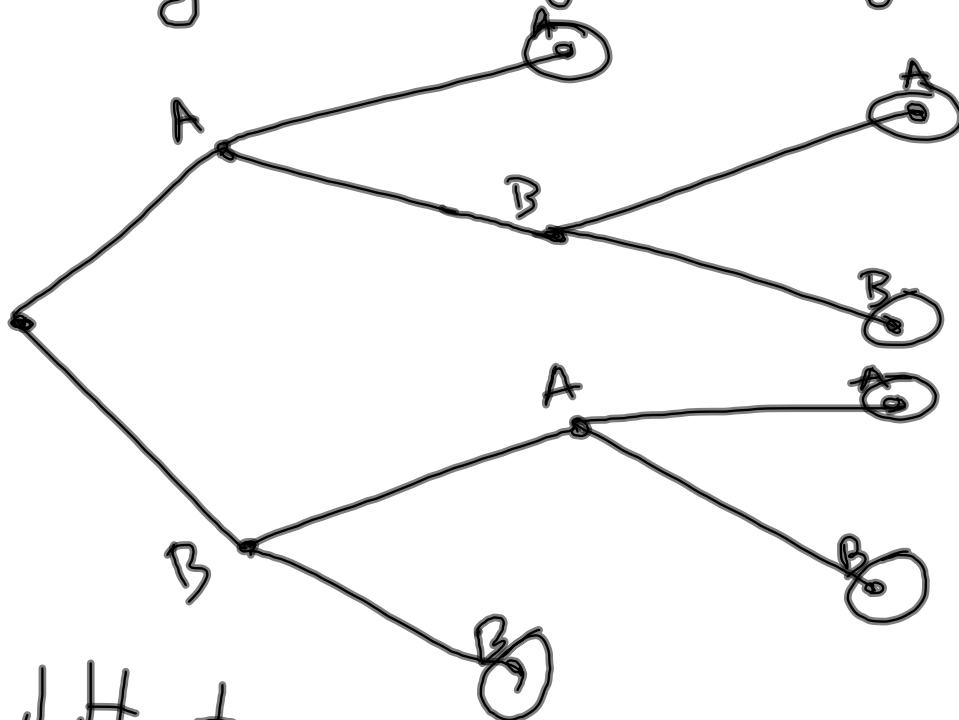
$$\text{total} = 333 - 34 + 1 = 300$$

probability that a 3 digit #
is divisible by 3

div by 3 → $\frac{300}{(999 - 100 + 1)} = \frac{300}{900} = \frac{1}{3}$

of 3 digit

Best of three tournament A v. B
 game 1 game 2 game 3



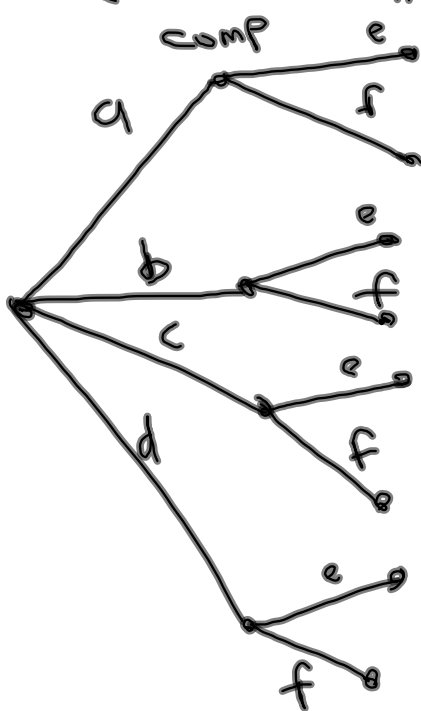
Possibility tree

6 different outcomes
 2 end in game 2

$$\frac{2}{6} = \frac{1}{3}$$

4 computers
 $C = \{a, b, c, d\}$ mon.

2 monitors
 $M = \{e, f\}$



$C \times M =$
 $\{(a, e), (a, f), (b, e),$
 $(b, f), (c, e), (c, f),$
 $(d, e), (d, f)\}$

Multiplication Rule

an operation consists of k steps

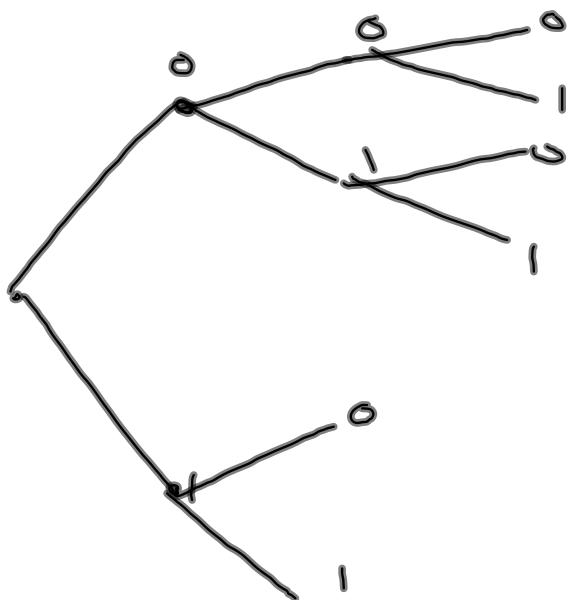
for each step i , step i can

be performed in n_i ways

the entire operation can be done
in $n_1 \cdot n_2 \cdot n_3 \cdot \dots \cdot n_k$ ways

Truth Table of n-variables?

var 1 v2 v3



$$2 \cdot 2 \cdot 2 \cdot \dots \cdot 2 = 2^n$$

Identifiers

- char, numbers, -
- starts w/ char, -

1st char ⁵³
{a..z, A..Z, -}

after ⁶³
{a..z, A..Z, -, 0..9}

ident. of length 3

53 · 63 · 63

~~2 var~~

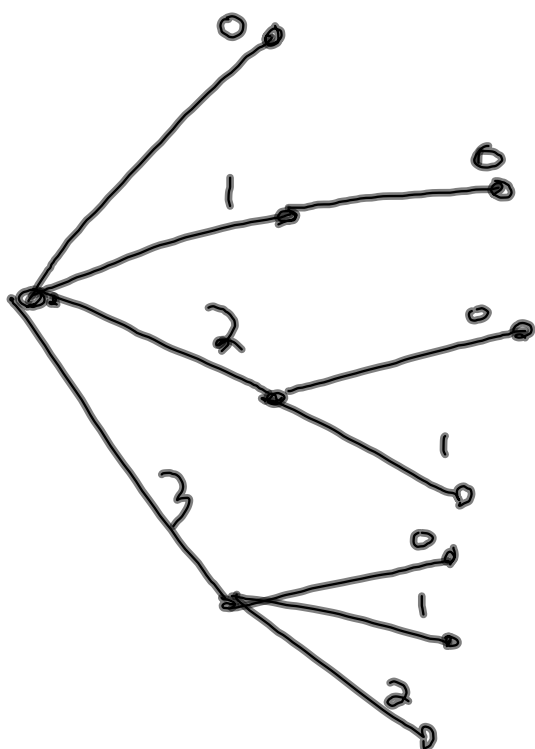
2L

2F

```
for (int i = 0; i < 4; i++)  
  for (int j = 0; j < 3; j++)  
    print('x');
```

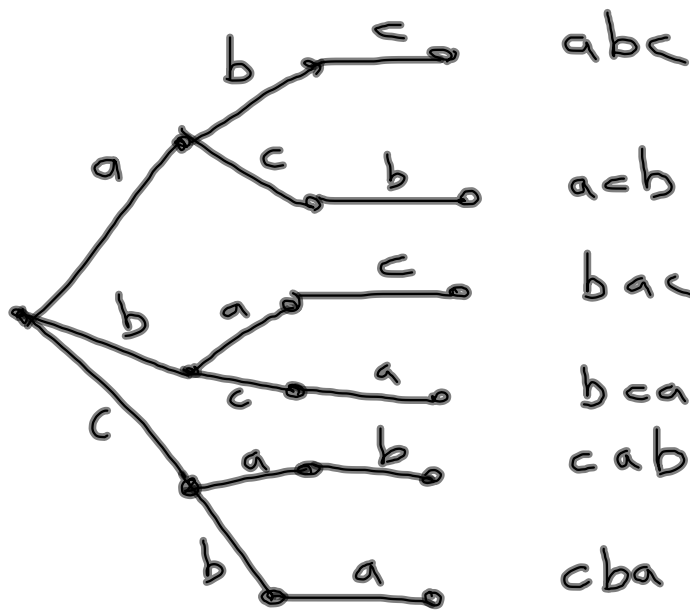
12 x's

```
for (int i = 0; i < 4; i++)  
  for (int j = 0; j < i; j++)  
    print('x');
```



6 x's

$$A = \{a, b, c\} = \{b, a, c\} = \dots$$



permutations
of A

$$3 \cdot 2 \cdot 1 = 6$$

for a set w/ n items
first item second 3rd

$$n \cdot (n-1) \cdot (n-2) \cdots 2 \cdot 1 \\ = n!$$

$A = \{a, b, c\}$
strings of length 2

$$\underline{3} \cdot \underline{2}$$

$\{ab, ac, ba, bc, ca, cb\}$

2-permutation
of A