

Subset Sum

$\{1, -2, 7\}$

$k = 5$

$\{\}$

$\{1\}$

$\{-2\}$

$\{7\}$

$\{1, -2\}$

$\{1, 7\}$

$\{-2, 7\}$

$\{1, -2, 7\}$

string 0's
1's

000 110

100 101

010 011

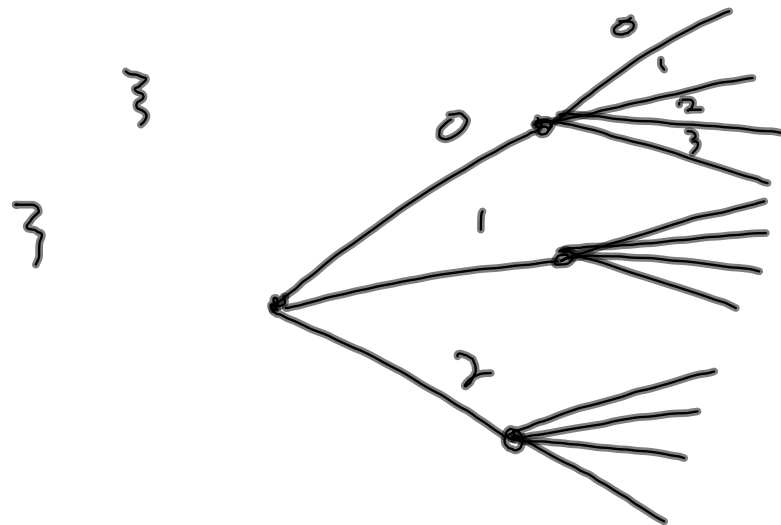
001 111

1. Test 2 was:
 - a. Too long
 - b. Too difficult
 - c. Neither a or b.
 - d. Both a and b.
2. Draw your favorite fruit.

```

n=3; m=4;
for(int i=0; i<n; i++){
    for(int j=0; j<m; j++){
        //statement
    }
}

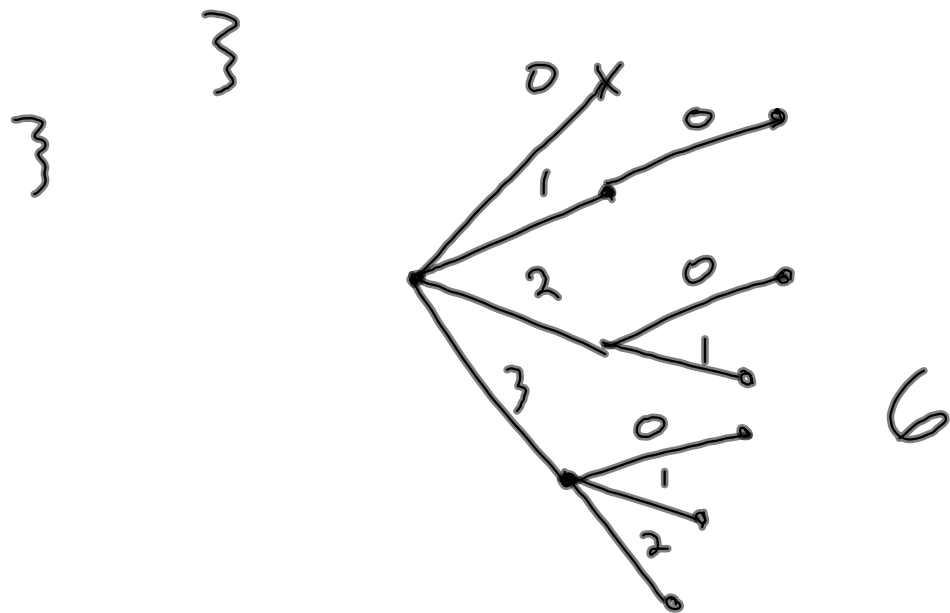
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```

for(int i=0; i<4; i++){
    for(int j=0; j<i; j++){
        //statement
    }
}

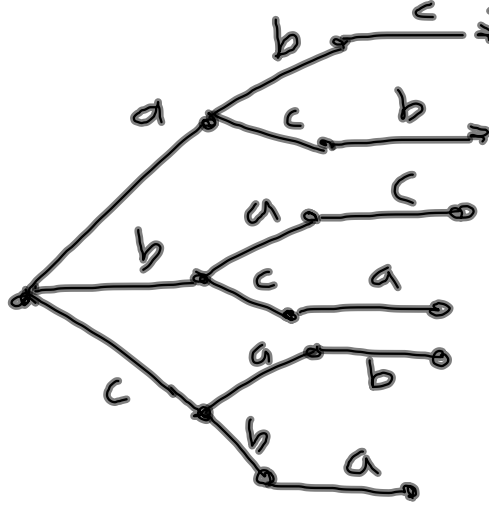
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Permutations

- different orderings of a set of objects.

$$S = \{a, b, c\}$$



$$3 \cdot 2 \cdot 1$$

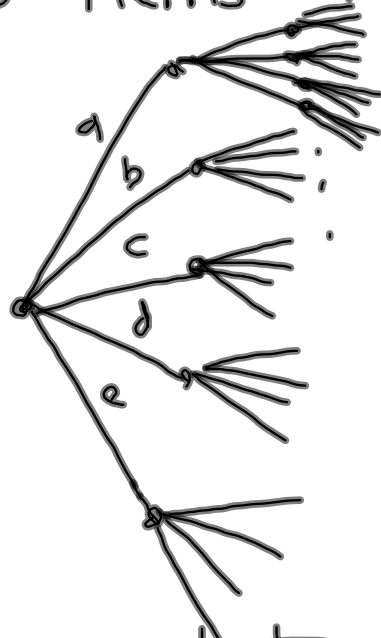
number of permutations

for n objects ($n \geq 1$)

$$n \cdot (n-1) \cdot (n-2) \cdots 2 \cdot 1 = n!$$

$$A = \{a, b, c, d, e\}$$

3 items (ordered)



$$5 \cdot 4 \cdot 3$$

3-perm of 5
objects

r -permutation of n objects

$$P(n, r) = n(n-1)(n-2) \dots \\ \dots (n-r+1)$$

$$= \frac{n!}{(n-r)!}$$

$$\frac{5 \cdot 4 \cdot 3 \cdot \cancel{2} \cdot \cancel{1}}{\cancel{2} \cdot \cancel{1}}$$

ALGORITHM

how many 3 letter "words"
can we make w/ ALGORITHM

$$P(9, 3) = \frac{9!}{6!} = 9 \cdot 8 \cdot 7$$

3-perm of
9 objects

Disjoint Sets

set A is a union of mutually disjoint sets

$$A_1, A_2, A_3, \dots A_k$$

$$N(A) = N(A_1) + N(A_2) + \dots N(A_k)$$

number of elements in A

number of "words" of 3 or fewer letters (a..z)

3 letters: $26 \cdot 26 \cdot 26 = 26^3$
2 letters: 26^2
1 letter: 26
0 letter?: 1

|||

$$26^3 + 26^2 + 26 + 1$$

Number of 3 digit numbers
divisible by 5

100, 101, 102, ...

$$\begin{array}{l} \text{└───} \\ 5 \cdot 20 \end{array}$$

995, ..., 999

$$\begin{array}{l} \text{└───} \\ 5 \cdot 199 \end{array}$$

$$199 - 20 + 1 = 180$$

3 digit ending in 0

$$9 \cdot 10 \cdot 1 = 90$$

ending in 5

$$9 \cdot 10 \cdot 1 = 90$$

$$90 + 90 = 180$$

Difference Rule

if A is finite and $B \subseteq A$
then

$$N(A - B) = N(A) - N(B)$$

3 letter words - (a..z)
 26^3

3 letter words (a..z) no repeats
 $26 \cdot 25 \cdot 24$

3 letter words w/ repeats
 $26^3 - 26 \cdot 25 \cdot 24$